

### Lecture 18: Approximate Pattern Matching

Study Chapter 9.6 – 9.8

#### Approximate vs. Exact Pattern Matching

- Previously we have discussed exact pattern matching algorithms
- Usually, because of mutations, it makes much more biological sense to find approximate pattern matches
- Biologists often use fast heuristic approaches (rather than local alignment) to find approximate matches



# Heuristic Similarity Searches

- Genomes are huge: Smith-Waterman quadratic alignment algorithms are too slow
- Observation: Good alignments of two sequences usually have short identical or highly similar subsequences
- Many heuristic methods (i.e., BLAST, FASTA) are based on the idea of *filtration* 
  - Find short exact matches, and use them as "seeds" for potential match extension
  - "Filter" out positions with no extendable matches



# Dot Plot

- A dot matrix or dot plot show similarities between two sequences
- FASTA makes an implicit dot matrix from short exact matches, and tries to find long diagonals (allowing for some mismatches)
- Nucleotide matches

	G	Α	Т	Т	С	G	С	Т	Т	Α	G	Т
С					*		*					
Т			*	*				*	*			*
G						*					*	
Α		*								*		
Т			*	*				*	*			*
Т			*	*				*	*			*
С					*		*					
С					*		*					
Т			*	*				*	*			*
Т			*	*				*	*			*
Α		*								*		
G						*					*	
Т			*	*				*	*			*
С					*		*					
Α		*								*		
G	*					*					*	
l = 1												
						ι =	= _	L				

# Dot Plot

- A dot matrix or dot plot show similarities between two sequences
- FASTA makes an implicit dot matrix from short exact matches, and tries to find long diagonals (allowing for some mismatches)
- Dinucleotide matches



### Dot Plot

- Identify diagonals above a threshold length
- Diagonals in the dot matrix indicate exact substring matching



# Diagonals in Dot Plots

- Extend diagonals and try to link them together, allowing for minimal mismatches/ indels
- Linking diagonals reveals approximate matches over longer substrings



#### A Realistic Dot-Plot

- On the right is a dot-plot of approximately ~200 KB of genomic sequence compared to itself.
- L = 20 with >= 90% concordance
- What to the off diagonal traces represent?



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#### Approximate Pattern Matching (APM)

- <u>Goal</u>: Find all approximate occurrences of a pattern in a text
- <u>Input</u>:
  - pattern **p** =  $p_1 \dots p_n$
  - $\operatorname{text} \mathbf{t} = t_1 \dots t_m$
  - the maximum number of mismatches *k*
- <u>Output</u>: All positions  $1 \le i \le (m n + 1)$  such that  $t_i \dots t_{i+n-1}$  and  $p_1 \dots p_n$  have at most k mismatches i.e., Hamming distance between  $t_i \dots t_{i+n-1}$  and  $\mathbf{p} \le k$



#### APM: A Brute-Force Algorithm

#### <u>ApproximatePatternMatching(p, t, k)</u>

- $n \leftarrow \text{length of pattern } \mathbf{p}$ 1
- 2  $m \leftarrow$  length of text t

**3** for 
$$i \leftarrow 1$$
 to  $m - n + 1$ 

4 
$$dist \leftarrow 0$$

5 for 
$$j \leftarrow 1$$
 to  $n$ 

$$\begin{array}{ll} 6 & \text{if } t_{i+j-1} \mathrel{!=} p_j \\ 7 & dist \leftarrow dist \mathrel{+} \end{array}$$

8 if 
$$dist \leq k$$



#### APM: Running Time

- That algorithm runs in O(*nm*).
- Extend "Approximate Pattern Matching" to a more general "Query Matching Problem":
  - Match *n*-length substring of the query (not the full pattern) to a substring in a text with at most *k* mismatches
  - Motivation: we may seek similarities to some gene, but not know which parts of the gene to consider



# Query Matching Problem

- <u>Goal</u>: Find all substrings of the query that approximately match the text
- <u>Input</u>: Query  $\mathbf{q} = q_1 \dots q_w$ , text  $\mathbf{t} = t_1 \dots t_m$ , *n* (length of matching substrings  $n \le w \le m$ ), *k* (maximum number of mismatches)
- <u>Output</u>: All pairs of positions (*i*, *j*) such that the *n*-letter substring of **q** starting at *i* approximately matches the *n*-letter substring of **t** starting at *j*, with at most *k* mismatches



#### Approximate Pattern Matching vs Query Matching







# Query Matching: Main Idea

- Approximately matching strings share some perfectly matching substrings.
- Instead of searching for approximately matching strings (difficult) search for perfectly matching substrings first (easy).



# Filtration in Query Matching

- We want all *n*-matches between a query and a text with up to *k* mismatches
- "Filter" out positions that do not match between text and query
- Potential match detection: find all matches of *l*-tuples in query and text for some small *l*
- **Potential match verification**: Verify each potential match by extending it to the left and right, until (*k* + 1) mismatches are found

# Filtration: Match Detection

- If  $x_1...x_n$  and  $y_1...y_n$  match with at most  $k \ll n$  mismatches they must share  $\ell$ -mers that are perfect matches, with  $\ell = \lfloor n/(k+1) \rfloor$
- Break string of length *n* into *k*+1 parts, each of length [*n*/(*k* + 1)]
  - k mismatches can affect at most k of these k+1 parts
  - At least one of these *k*+1 parts is perfectly matched



#### Filtration: Match Detection (cont'd)

• Suppose k = 3. We would then have l=n/(k+1)=n/4:



• There are at most *k* mismatches in *n*, so at the very least there must be one out of the *k*+1 *l*-tuples without a mismatch



### Filtration: Match Verification

• For each *l*-match we find, try to extend the match further to see if it is substantial



#### Filtration: Example

	<b>k</b> = 0	<b>k</b> = 1	<i>k</i> = 2	<b>k</b> = 3	<b>k</b> = 4	<b>k</b> = 5
l∕-tuple length	п	<i>n</i> /2	<b>n</b> /3	<b>n</b> /4	<b>n</b> /5	<b>n</b> /6

Shorter perfect matches required

#### Performance decreases

# Local alignment is too slow...

- Quadratic local alignment is too slow when looking for similarities between long strings (e.g. the entire GenBank database)
- Guaranteed to find the optimal local alignment
- Sets the standard for sensitivity
- Basic Local Alignment Search Tool
  - Altschul, S., Gish, W., Miller, W., Myers, E. & Lipman, D.J.
    Journal of Mol. Biol., 1990
- Search sequence databases for local alignments to a query

$$S_{i,j} = \max \begin{cases} 0\\ s_{i-1,j} + \delta(v_i, -)\\ s_{i,j-1} + \delta(-, w_j)\\ s_{i-1,j-1} + \delta(v_i, w_j) \end{cases}$$

# BLAST

- Great improvement in speed, with only a modest decrease in sensitivity
- Opts to minimizes search space instead of exploring entire search space between two sequences
- Finds short exact matches ("seeds"), explore locally around these "hits"



Search space of Local Alignment







# Similarity

- BLAST only continues it's search as long as regions are sufficiently *similar*
- Measuring the extent of similarity between two sequences
  - Based on percent sequence <u>identity</u>
  - Based on <u>conservation</u>



# Percent Sequence Identity

• The extent to which two nucleotide or amino acid sequences are invariant



### Conservation

- Amino acid changes that preserve the physicochemical properties of the original residue
  - Polar to polar
    - aspartate  $\rightarrow$  glutamate
  - Nonpolar to nonpolar
    - alanine  $\rightarrow$  valine
  - Similarly behaving residues
    - leucine to isoleucine
- Nucleotide changes that preserve molecular shape
  - Transitions (A-G, C-T) are more similar than Transversions (A-C, A-T, C-G, G-T)



# Assessing Sequence Similarity

- How good of a local alignment score can be expected from chance alone
- "Chance" relates to comparison of sequences that are generated randomly based upon a certain sequence model
- Sequence models may take into account:
  - nucleotide frequency
  - dinucelotide frequency
    - (e.g. C+G content in mammals)
  - common repeats

– etc.



# **BLAST: Segment Score**

- BLAST uses scoring matrices (δ) to improve on efficiency of match detection (we did this earlier for pairwise alignments)
  - Some proteins may have very different amino acid sequences, but are still similar (PAM, Blosum)
- For any two  $\ell$ -mers  $x_1...x_l$  and  $y_1...y_l$ :
  - <u>Segment pair</u>: pair of *l*-mers, one from each sequence

- Segment score: 
$$\Sigma_{i=1}^{\ell} \delta(x_i, y_i)$$

# BLAST: Locally Maximal Segment Pairs

- A segment pair is <u>maximal</u> if it has the best score over all segment pairs
- A segment pair is <u>locally maximal</u> if its score can't be improved by extending or shortening
- Statistically significant *locally maximal* segment pairs are of biological interest
- BLAST finds all locally maximal segment pairs (MSPs) with scores above some threshold
  - A significantly high threshold will filter out some statistically insignificant matches



#### **BLAST: Statistics**

- Threshold: Altschul-Dembo-Karlin statistics
  - Identifies smallest segment score that is unlikely to happen by chance
- # matches above  $\theta$  has mean (Poission-distributed):

 $\mathbf{E}(\boldsymbol{\theta}) = Kmne^{-\lambda\boldsymbol{\theta}}$ 

*K* is a constant, *m* and *n* are the lengths of the two compared sequences,  $\lambda$  is a positive root of:

$$\Sigma_{x,y\,in\,A}(p_xp_ye^{\delta(x,y)})=1$$

where  $p_x$  and  $p_y$  are frequencies of amino acids x and y,  $\delta$  is the scoring matrix, and A is the twenty letter amino acid alphabet

### P-values

- The probability of finding exactly *k* MSPs with a score  $\geq \theta$  is given by:  $(E(\theta)^k e^{-E(\theta)})/k!$
- For *k* = 0, that chance is:

 $e^{-E(\theta)}$ 

• Thus the probability of finding at least one MSP with a score  $\ge \theta$  is:

$$p(MSP > 0) = 1 - e^{-E(\theta)}$$



# BLAST algorithm

• Keyword search of all substrings of length *w* from the query of length *n*, in database of length *m* with score above threshold

-w = 11 for DNA queries, w = 3 for proteins

- Local alignment extension for each found keyword
  - Extend result until longest match above threshold is achieved
- Running time O(*nm*)





keyword

Query: KRHRKVLRDNIQGITKPAIRRLARRGGVKRISGLIYEETRGVLKIFLENVIRD



# Original BLAST

- Dictionary
  - All words of length *w*
- Alignment
  - <u>Ungapped</u> extensions until score falls below some statistical threshold
- Output
  - All local alignments with score > threshold



# Original BLAST: Example

- w = 4
- Exact keyword match of **GGTC**
- Extend diagonals with mismatches until score is under some threshold (65%)
- Trim to until all mismatches are interior
- Output result: GTAAGGTCC II IIIII GTTAGGTCC

From lectures by Serafim Batzoglou (Stanford) 11/5/13



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# Gapped BLAST : Example

- Original BLAST exact keyword search, then:
- Extend with gaps around ends of exact match until score < threshold</li>
- Output result:

GTAAGGTCCAGT || |||| ||| GTTAGGTC-AGT

From lectures by Serafim Batzoglou (Stanford)

⋖ U U G ⊢ ⊢ ◄ σ U ⊢ U C ⊢ ◄ σ ⊢ U

A C G A A G T A A G G T C C A G T

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### Incarnations of BLAST

- blastn: Nucleotide-nucleotide
- blastp: Protein-protein
- blastx: Translated query vs. protein database
- tblastn: Protein query vs. translated database
- tblastx: Translated query vs. translated database (6 frames each)



# Incarnations of BLAST (cont'd)

- PSI-BLAST
  - Find members of a protein family or build a custom position-specific score matrix
- Megablast:
  - Search longer sequences with fewer differences
- WU-BLAST: (Wash U BLAST)
  - Optimized, added features



### Sample BLAST output

#### Blast of human beta globin protein against zebra fish

Sequences producing significant alignments:	Score	E (bits)	Value					
gi 18858329 ref NP_571095.1  ba1 globin [Danio rerio] >gi 147757 gi 18858331 ref NP_571096.1  ba2 globin; SI:dZ118J2.3 [Danio rer gi 37606100 emb CAE48992.1  SI:bY187G17.6 (novel beta globin) [D gi 31419195 gb AAH53176.1  Ba1 protein [Danio rerio]	171 170 170 168	3e-44 7e-44 7e-44 3e-43						
ALIGNMENTS >gi 18858329 ref NP_571095.1  bal globin [Danio rerio] Length = 148								
Score = 171 bits (434), Expect = 3e-44 Identities = 76/148 (51%), Positives = 106/148 (71%), Gaps = 1/148 (0%)								
Query: 1 MVHLTPEEKSAVTALWGKVNVDEVGGEALGRLLVVYPWTQRFFESFGDLSTPDAVMG	NDK 60							
Sbjct: 1 MVEWTDAERTAILGLWGKLNIDEIGPQALSRCLIVYPWTQRYFATFGNLSSPAAIMG	NPK 60							
Query: 61 VKAHGKKVLGAFSDGLAHLDNLKGTFATLSELHCDKLHVDPENFRLLGNVLVCVLAH	HFG 120							
Sbjct: 61 VAAHGRTVMGGLERAIKNMDNVKNTYAALSVMHSEKLHVDPDNFRLLADCITVCAAM	KFG 120							
Query: 121 KE-FTPPVQAAYQKVVAGVANALAHKYH 147								
Sbjct: 121 QAGFNADVQEAWQKFLAVVVSALCRQYH 148								

#### Sample BLAST output (cont'd)

#### • Blast of human beta globin DNA against human DNA

	6 6	Score	Е					
Sequences pr	oducing significant alignments:		(bits)	Value				
gi 19849266  gi 183868 gb gi 44887617  gi 31726 emb gi 38683401  gi 18462073	gb AF487523.1  Homo sapiens gamma A hemoglobin (HBG1  M11427.1 HUMHBG3E Human gamma-globin mRNA, 3' end gb AY534688.1  Homo sapiens A-gamma globin (HBG1) ge  V00512.1 HSGGL1 Human messenger RNA for gamma-globin ref NR_001589.1  Homo sapiens hemoglobin, beta pseud gb AF339400.1  Homo sapiens haplotype PB26 beta-glob	289 289 280 260 151 149	1e-75 1e-75 1e-72 1e-66 7e-34 3e-33					
ALIGNMENTS >gi 28380636 ref NG_000007.3  Homo sapiens beta globin region (HBB@) on chromosome 11 Length = 81706 Score = 149 bits (75), Expect = 3e-33 Identities = 183/219 (83%) Strand = Plus / Plus								
Query: 267 ttgggagatgccacaaagcacctggatgatctcaagggcacctttgcccagctgagtgaa 326 								
Query: 327	ctgcactgtgacaagctgcatgtggatcctgagaacttc 365							

Sbjct: 54469 ctgcactgtaacaagctgcacgtggaccctgagaacttc 54507



### Timeline

- 1970: Needleman-Wunsch global alignment algorithm
- 1981: Smith-Waterman local alignment algorithm
- 1985: FASTA
- 1990: BLAST (basic local alignment search tool)
- 2000s: BLAST has become too slow in "genome vs. genome" comparisons new faster algorithms evolve!
  - Pattern Hunter
  - BLAT



#### PatternHunter: faster and even more sensitive

- BLAST: matches short consecutive sequences (consecutive seed)
- Length = k
- Example (k = 11):

#### 111111111111

Each 1 represents a "match"

- PatternHunter: matches short non-consecutive sequences (spaced seed)
- Increases sensitivity by locating homologies that would otherwise be missed
- Example (a spaced seed of length 18 w/ 11 "matches"):

#### 111010010100110111

Each 0 represents a "don't care", so there can be a match or a mismatch



Spaced seeds

Example of a hit using a spaced seed:

#### 

How does this result in better sensitivity?



### Why is PH better?

#### BLAST redundant hits

#### TTGACCTCACC? |||||||||| TTGACCTCACC? 1111111111 1111111111

This results in > 1 hit and creates clusters of redundant hits

#### PatternHunter

CAA?A??A?C??TA?TGG? |||?|??|?||?||? CAA?A??A?C??TA?TGG? 111010010100110111 111010010100110111

This results in very few redundant hits



11/5/13

# Why is PH better?

#### **BLAST** may also miss a hit

# GAGTACTCAACACCAACATTAGTGGGCAATGGAAAAT

In this example, despite a clear homology, there is no sequence of continuous matches longer than length 9. BLAST uses a length 11 and because of this, BLAST does not recognize this as a hit!

Resolving this would require reducing the seed length to 9, which would have a damaging effect on speed



# Advantage of Gapped Seeds



# Why is PH better?

- Higher hit probability
- Lower expected number of random hits



# Use of Multiple Seeds

#### **Basic Searching Algorithm**

- 1. Select a group of spaced seed models
- 2. For each hit of each model, conduct extension to find a homology.



### Another method: BLAT

- BLAT (BLAST-Like Alignment Tool)
- Same idea as BLAST locate short sequence hits and extend



### BLAT vs. BLAST: Differences

- BLAT builds an index of the database and scans linearly through the query sequence, whereas BLAST builds an index of the query sequence and then scans linearly through the database
- Index is stored in RAM which is memory intensive, but results in faster searches



# BLAT: Fast cDNA Alignments

Steps:

- 1. Break cDNA into 500 base chunks.
- 2. Use an index to find regions in genome similar to each chunk of cDNA.
- 3. Do a detailed alignment between genomic regions and cDNA chunk.
- 4. Use dynamic programming to stitch together detailed alignments of chunks into detailed alignment of whole.

#### A sophisticated divide and conquer approach



#### However...

• BLAT was designed to find sequences of 95% and greater similarity of length >40; may miss more divergent or shorter sequence alignments



#### PatternHunter and BLAT vs. BLAST

- PatternHunter is 5-100 times faster than Blastn, depending on data size, at the same sensitivity
- BLAT is several times faster than BLAST, but best results are limited to closely related sequences

