Comp 555 - BioAlgorithms - Spring 2021

Q5E940_BOVIN	MPREDRATWKSNYFLKIIQLLDD <mark>YP</mark> KCFIVGADNVGSKQMQQIRMSLRGK-AVVLMGKNTMMRKAIRGHLENNPALE	76
RLA0 HUMAN	MPREDRATWKSNYFLKIIQLLDD <mark>YP</mark> KCFIVGADNVGSKQMQQIRMSLRGK-AVVLMGKNTMMRKAIRGHLENNPALE	76
RLA0 MOUSE	MPREDRATWKSNYFLKIIQLLDDYPKCFIVGADNVGSKQMQQIRMSLRGK-AVVLMGKNTMMRKAIRGHLENNPALE	76
RLA0_RAT	MPREDRATWKSNYFLKIIQLLDD <mark>YP</mark> KCFIVGADNVGSKQMQQIRMSLRGK-AVVLMGKNTMMRKAIRGHLENNPALE	76
RLA0 CHICK	MPREDRATWKSNYFMKIIQLLDDYPKCFVVGADNVGSKQMQQIRMSLRGK-AVVLMGKNTMMRKAIRGHLENNPALE	76
RLAO RANSY	MPREDRATWKSNYFLKIIQLLDDYPKCFIVGADNVGSKQMQQIRMSLRGK-AVVLMGKNTMMRKAIRGHLENNSALE	76
Q7ZUG3 BRARE	MPREDRATWKSNYFLKIIQLLDDYPKCFIVGADNVGSKQMQTIRLSLRGK-AVVLMGKNTMMRKAIRGHLENNPALE	76
RLA0 ICTPU	MPREDRATWKSNYFLKIIQLLNDYPKCFIVGADNVGSKQMQTIRLSLRGK-AIVLMGKNTMMRKAIRGHLENNPALE	76
RLA0 DROME	WVRENKAAW <mark>K</mark> AQYFIKVV <mark>E</mark> LFDEF <mark>P</mark> KCFIVGADNVGSK <mark>QMQ</mark> NI R TSL <mark>RG</mark> L-AVVLMGKNTMMRKAIRGHLENNPQLE	76
RLA0 DICDI	MSGAG-SKR <mark>K</mark> KLFIEKATKLFTTYDKMIVAEADFVGSSQLQKIRKSIRGI-GAVLMGKKTMIRKVIRDLADSKPELD	75
Q54LP0 DICDI	MSG AG - SKRKNVF IEKATKLFTT YDKMIV AE ADFVGS SQLQK IRKS IRG I - GAVLMGKKTMIRKVIRDLADSK - PELD	75
RLAO PLAF8	MAKLSKQQK <mark>K</mark> QMYIEKLSSLIQQYSKILIVHVDNVGSNQMASVRKSLRGK-ATILMGKNTRIRTALKKNLQAVPQIE	76
RLA0 SULAC	MIGLAVTTTKKIAKWKVDEVAELTEKLKTHKTIIIANIEGFPADKLHEIRKKLRGK-ADIKVTKNNLFNIALKNAGYDTK	79
RLA0 SULTO	MRIMAVITQERKIAKW <mark>K</mark> IEEVKELE <mark>Q</mark> KLREYHTIIIANI <mark>EGFP</mark> ADKLHDI <mark>R</mark> KKM <mark>RGM-AEIKVTKNTLFG</mark> IAAKNAGLDVS	80
RLA0 SULSO	MKRLALALKQRKVASW <mark>K</mark> LEEVKELT <mark>E</mark> LIKNSNTILIGNLEGFPADKLHEIRKKLRGK-ATIKVTKNTLFKIAAKNAGIDIE	80
RLA0 AERPE	MSVVSLV <mark>G</mark> QMYKREK <mark>PIPEWK</mark> TLMLRELE <mark>ELFSKHRVVLFADLTGTPT</mark> FVV <mark>Q</mark> RV <mark>R</mark> KKLWKK- <mark>YPMMVAKKRIILRAMKAAG</mark> LELDDN	86
RLA0 PYRAE	-MMLAIGKRRYWRTRQYPARKWKIVSEATELLQKYPYWFLFDLHGLSSRILHEYRYRLRRY-GVIKIIKPTLFKIAFTKVYGGIPAE	85
RLA0 METAC	MAEERHHTEH IPQWKKDE IEN IKEL IQSHK VFGM VG IEG ILATKMOK IRRD LKD V-AVLK VSRNTLTE RALNOLGET IP	78
RLAO METMA	MAEERHHTEHI <mark>P</mark> QW <mark>K</mark> KDEIENIK <mark>E</mark> LIQSHKVFGMVRIEGILATKI <mark>Q</mark> KIRRDLKDV-AVLKVSRNTLTERALNQLGESIP	78
RLA0 ARCFU	MAAVRGSPPEYKYRAVEEIKRMISSKPVVAIVSFRNVPAGOMOKIRREFRGK-AEIKVVKNTLLERALDALGGDYL	75
RLA0 METKA	MAVKAK <mark>GOPP</mark> SGYE <mark>P</mark> KVAEWKRREVKELK <mark>E</mark> LMDEYENVGLVDLEGIPAPOLOEIRAKLRERDTIIRMSRNTLMRIALEEKLDERPELE	88
RLA0 METTH	MAHVAEWKKKEVQELHDLIKGYEVVGIANLADIPARQLQKMRQTLRDS-ALIRMSKKTLISLALEKAGRELENVD	74
RLA0 METTL	MITAE SE HK IAPWK IE E VNKLKELLKNGQIVAL VDMME VPARQLQE IRDK IR-GTMTLKMSRNTLIE RAIKE VAE ET GNPE FA	82
RLA0 METVA	MIDAKSEHKIA <mark>PWK</mark> IEEVNALK <mark>E</mark> LLKSANVIALIDMMEVPAVQLQEIRDKIR-DQMTLKMSRNTLIKRAVEEVAEETGNPEFA	82
RLA0 METJA	METKVKAHVAPWKIEEVKTLKGLIKSKPVVAIVDMMDVPAPQLQEIRDKIR-DKVKLRMSRNTLIIRALKEAAEELNNPKLA	81
RLA0 PYRAB	MAHVAEWKKKEVEELANLIKSYPVIALVDVSSMPAYPLSQMRRLIRENGGLLRVSRNTLIELAIKKAAQELGKPELE	77
RLA0 PYRHO	MAHVAEWKKKEVEELAKLIKS <mark>YP</mark> VIALVDVSSMPAYPLSQMRRLIRENGGLLRV <mark>SRNT</mark> LIELAIKKAAKEL <mark>GKP</mark> ELE	77
RLA0 PYRFU	MAHVAEW <mark>K</mark> KKEVEELANLIKSY <mark>P</mark> VVALVDVSSMPAYPLSQMRRLIRENNGLLRVSRNTLIELAIKKVAQELGKPELE	77
RLA0 PYRKO	MAHVAEWKKKEVEELANIIKS <mark>YP</mark> VIALVDVAGVPAYPLSKMRDKLR-GKALLRVSRNTLIELAIKRAAQELGQPELE	76
RLA0 HALMA	MSAESERKTETIPEWKQEEVDAIVEMIESYESVGVVNIAGIPSRQLQDMRRDLHGT-AELRVSRNTLLERALDDVDDGLE	79
RLA0 HALVO	MSESEVRQTEVIPQWKREEVDELVDFIESYESVGVVGVAGIPSRQLQSMRRELHGS-AAVRMSRNTLVNRALDEVNDGFE	79
RLA0 HALSA	MSAEEQRTTEEVPEWKRQEVAELVDLLETYDSVGVVNVTGIPSKQLQDMRRGLHGQ-AALRMSRNTLLVRALEEAGDGLD	79
RLA0 THEAC	MKEVSQQKKELVNEITQRIKASRSVAIVDTAGIRTRQIQDIRGKNRGK-INLKVIKKTLLFKALENLGDEKLS	72
RLA0 THE VO	MRKIN <mark>P</mark> KKKEIVSELAQDITKSKAVAIVDIKGVR <mark>T</mark> RQMQDIRAKNRDK-VKIKVVKKTLLFKALDSINDEKLT	72
RLA0 PICTO	MTEPAQWKIDFVKNLENE INSRKVAAIVSIKGLRNNEFOKIRNSIRDK-ARIKV <mark>SR</mark> ARLLRLAIENTGKNNIV	72
ruler	110203040	

- PROBLEM SET #2 15 GRADED
- MIDTERM GRADES WILL BE RELEASED NEXT TUESDAY.
- TALK TODAY AFTER CLASS: PEI-CHEN PENG https://zoom.us/j/98724499419

Comparing Sequences

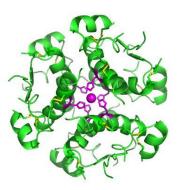
Sequence Similarity



• A common problem in biology

	Insulin Protein Sequence
Human	MALWMRLLPLLALLALWGPDPAAAFVNQHLCGSHLVEALYLVCGERGFFYTPKTRREAEDLQGSLQPLALEGSLQKRGIVEQCCTSICSLYQLENYCN
Dog	MALWMRLLPLLALLALWAPAPTRAFVNQHLCGSHLVEALYLVCGERGFFYTPKARREVEDLQVRDVELAGAPGEGGLQPLALEGALQKRGIVEQCCTSICSLYQLENYCN
Cat	MAPWTRLLPLLALLSLWIPAPTRAFVNQHLCGSHLVEALYLVCGERGFFYTPKARREAEDLQGKDAELGEAPGAGGLQPSALEAPLQKRGIVEQCCASVCSLYQLEHYCN
Pig	MALWTRLLPLLALLALWAPAPAQAFVNQHLCGSHLVEALYLVCGERGFFYTPKARREAENPQAGAVELGGGLGGLQALALEGPPQKRGIVEQCCTSICSLYQLENYCN

- All similar, but how similar?
- How do you measure similarity?
- Does Hamming distance work here?
- Uses
 - To establish a *phylogeny*
 - To identify *functional* or *conserved* components of the sequence



Hand Alignments



- Not that long ago, many alignments were done by hand
- - AFVNQHLCGSHLVEALYLVCGERGFFYTPKARREAE QKRGIVEQCC SICSLYQLENYCN
 - Long conserved regions are shown below
 - Solution strategy?
- Is this a well defined problem?
 - Is there an optimal or best solution?
 - Did we find it?
- By the way, this is an easy case. Within vertebrates, the amino acid sequence of insulin is strongly conserved.

The Alignment Game



Let's consider only 2 sequences, and establish "alignment" rules as if it were a game.

- Rules:
 - You must remove all characters from both sequences
 - There are 3 possible moves at any point in the game.
 - Each move removes at least one character from one of the two given strings
 - Pressing [Match] removes one left-most character from both sequences
 - You get 1 point if the characters match, otherwise you get 0 points
 - Pressing [Del] removes the left-most character from the top sequence
 - You lose 1 point
 - Pressing [Ins] removes the left-most character from the bottom sequence
 - You lose 1 point
 - \circ \quad Your point total is allowed to go negative
- Objective: Get the most points



How do you get the highest possible score?

- The solution may not be unique
- How many presses?
 - Minimum moves = Max(len(top), len(bot))
 - Maximum moves = len(top) + len(bot)
- How many possible moves?
 - Less than 3^{len(top) + len(bot)}
- How big for our problem instance?
 - len(Human) = 98, len(dog) = 110
 - $3^{208} \approx 1.73 \times 10^{90}$, almost a googol (not a google)
- What algorithm solves this problem?
 - Make each move by considering only a short horizon following the current aligment thus far



There is an efficient solution



- It relies on a rather surprising idea
- The best score can be found for the len(top) and len(bot) strings by finding the best score for every pair of substrings len(top[0:n]) and len(bot[0:m]) for all values of n up to len(top) and m up to len(bot)
- Finding this solution requires only O(len(top)len(bot)) steps
- It also requires a table of size Max(len(top),len(bot))
- But before we solve this problem, let's look at another related related problem

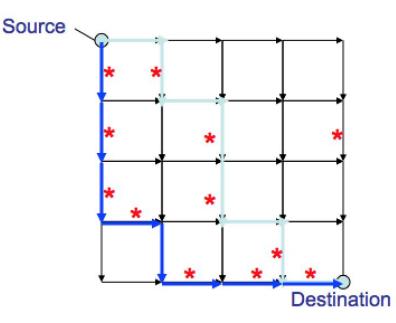
Finding a best city tour on a Manhattan grid



Manhattan Tourist Problem (MTP)



Imagine seeking a path from a given source to given destination in a Manhattan-like city grid that maximizes the number of attractions (*) passed. With the following caveat- at every step you must make progress towards the goal. We treat the city map as a graph, with a *vertices* at each intersection, and *weighted edges* along each block. The weights are the number of attractions along each block.



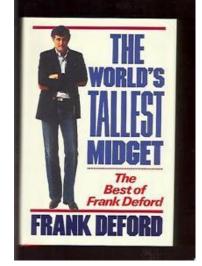
Manhattan Tourist Game

Goal: Find the maximum weighted shortest path in a grid.

Input: A weighted grid G with two distinct vertices, one labeled *source* and the other labeled *destination*

Output: A shortest path in G from source to destination with the greatest weight

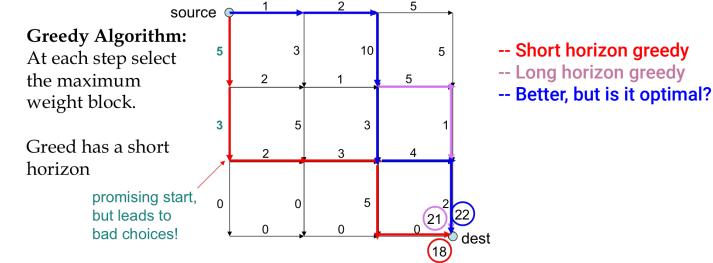
- There are many *shortest* paths that go south 4 blocks and east 4 blocks
- Of those paths, which sees the most sites?







MTP: A Greedy Algorithm Is Not Optimal



Different types of Greedy

- Short horizon: At each block select the direction where the next block offers the most attractions
- Long horizon: Look ahead at all streets between your current position and the destination, and then go down streets with the most attractions

A New Solution Strategy



Dynamic Programming is a technique for computing recurrence relations efficiently by storing and reusing intermediate results

Three keys to constructing a dynamic programming solution:

- 1. Formulate the answer as a recurrence relation
- Consider all instances of the recurrence at each step (In our case this means all paths that lead to a vertex or intersection).
- 3. Order evaluations so you will always have precomputed any needed partial results
- **Irony:** Often the most efficient approach to solving a specific problem involves solving *every* smaller subproblem.

MTP Dynamic Program Solution



source З 3 0 Δ from: з 22 5 destination

In this case our smaller subproblems are finding the optimal path to "every" intersection that lies between our source and destination.

Where the optimal path to (i,j) is the better of the optimal paths

(i-1,j) to (i,j) or (i,j-1) to (i,j), because those are the only ways to get to (i,j)

The solution may not be unique, but it will have the best possible, optimal, score

MTP Dynamic Program Strategy



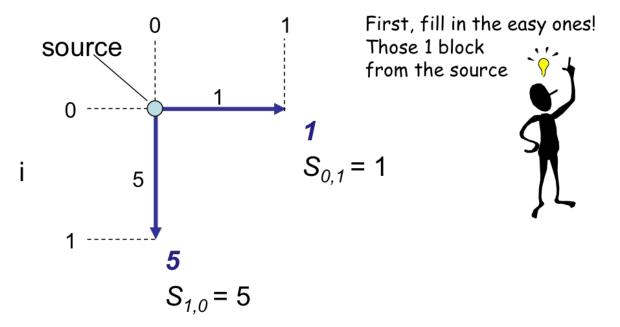
- Instead of solving the Manhattan Tourist problem directly, (i.e. the path from (0,0) to (n,m)) we will solve a more general problem: find the longest path from (0,0) to any arbitrary vertex (i,j).
- If the longest path from (0,0) to (n,m) passes through some vertex (i,j), then the path from (0,0) to (i,j) must be the longest. Otherwise, you could increase the weight along your path by changing it.



MTP: Dynamic Program



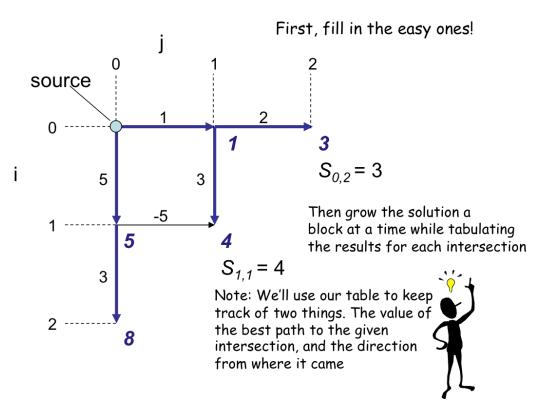
- Calculate optimal path score for *every* vertex in the graph between our source and destination
- Each vertex's score is the maximum of the prior vertices score plus the weight of the connecting edge in between





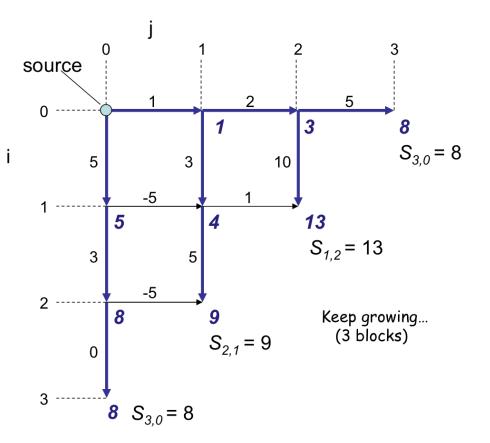
Consider all destinations 2 blocks from the source.

Notice I have allowed "negative" edge weights... assume these are the number of things that your guide book suggests you should avoid at all cost!

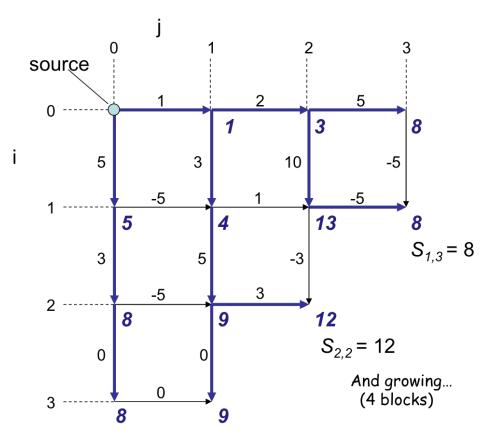


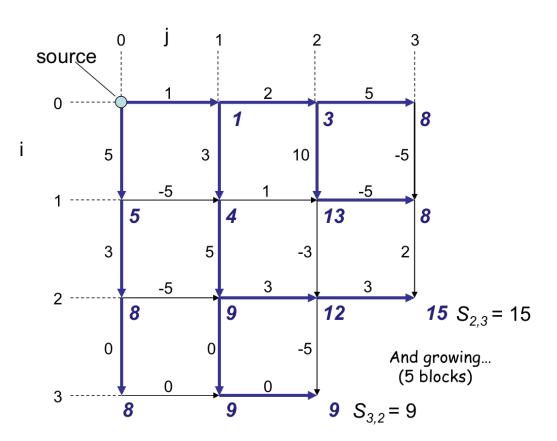


For each intersection let's keep track of the score and the direction that our "best" answer came from... We could do this by putting a yellow sticky on a corner lamp post, which said we saw *N* sites and arrived from either the north or the west

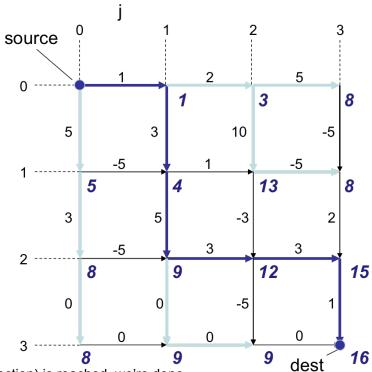












- Once the *destination* node (intersection) is reached, we're done.
- Our table will have the answer of the maximum number of attractions stored in the entry associated with the destination.
- We use the *links* back in the table to recover the path. (Backtracking)

Comp 555 - Spring 2021

MTP: Recurrence



Computing the score for a point (i,j) by the recurrence relation:

$$s_{i,j} = \max \begin{cases} s_{i-1,j} + \text{weight of the edge between } (i-1,j) \text{ and } (i,j) \\ s_{i,j-1} + \text{weight of the edge between } (i,j-1) \text{ and } (i,j) \\ \end{cases}$$

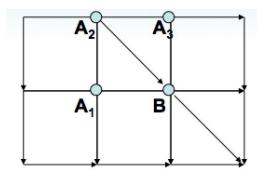
The running time is *nm* for a n × m grid

• You visit all intersections once, add two numbers, compare which is larger, save it and it's direction

(n = # of rows, m = # of columns)

Manhattan Is Not A Perfect Grid





1

What about diagonals? Broadway, Greenwich, etc.

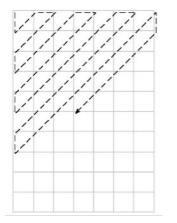
- Easy to fix. Just adds more recursion cases.
- The score at point B is given by:

$$s_{B} = \max \begin{cases} s_{A1} + \text{weight of the edge } (A_{1}, B) \\ s_{A2} + \text{weight of the edge } (A_{2}, B) \\ s_{A3} + \text{weight of the edge } (A_{3}, B) \end{cases}$$

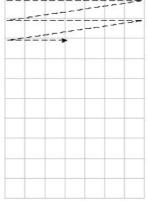
Other ways to safely explore the Manhattan

They want

- We chose to evaluate our table in a particular order. Uniform distances from the source (all points one block away, then 2 blocks, etc.)
- Other strategies:
 - Column by column
 - Row by row
 - Radiate out along diagonals
- This choice can have performance implications







Next Time



- Return to sequence alignment
- Coding dynamic programs

