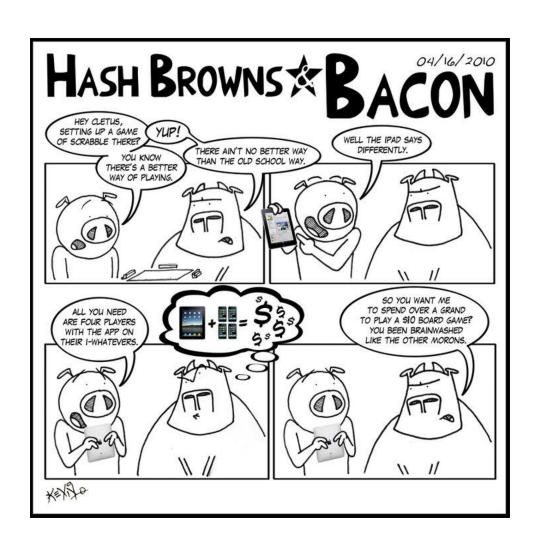




### Hash-Based Indexes

Chapter 11







#### Introduction

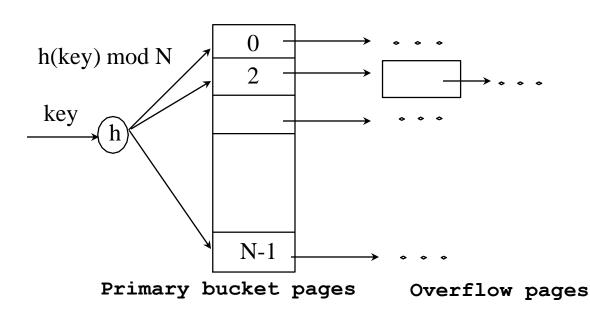
- \* Hashing maps a search key directly to the pid of the containing page/page-overflow chain
- Doesn't require intermediate page fetches for internal "steering nodes" of tree-based indices
- \* <u>Hash-based</u> indexes are best for *equality selections*. They do not support efficient range searches.
- Static and dynamic hashing techniques exist with trade-offs similar to ISAM vs. B+ trees.





### Static Hashing

- # primary index pages fixed, allocated sequentially, never de-allocated; overflow pages if needed.
- \*  $h(k) \mod M$  = bucket to which data entry with key k belongs. (M = # of buckets)







# Static Hashing (Contd.)

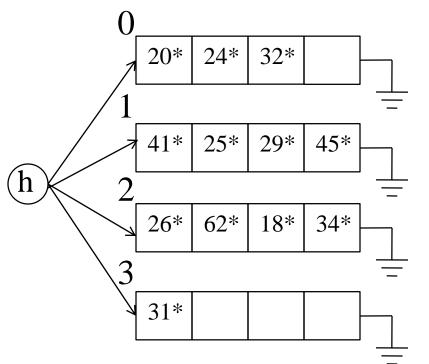
- ❖ Buckets contain data entries (<search key>, <rid>).
- \* Hash function maps a search key to a bin number  $h(key) \rightarrow 0 \dots M-1$ . Ideally uniformly.
  - in practice  $h(key) = (A * key + B) \mod M$ , works well.
  - Where A and B are relatively prime constants
  - Lots of research about how to tune h.
- Long overflow chains can develop and degrade performance.
- \* Hence, dynamic hashing techniques (*Extendible* and *Linear Hashing*) address this problem.





# Static Hashing Example

\* Initially built over "Ages" attribute of our Sailing club database, with 4 records/page and h(Age) = Age mod 4



**Initial Index** 

Note: records need not be ordered

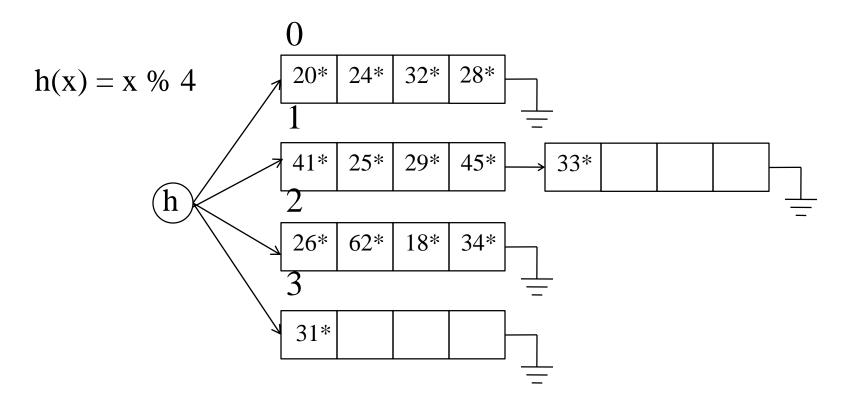
Average Occupancy?





# Static Hashing Example

- \* Adding 28, 33
- Deleting 31, (leads to empty page)







# Hashing's "Achilles Heel"

- Maintaining Balance
  - Data is often "clustered"
  - Ideal hash functions should uniformly distribute keys over buckets. Demands a good hash function (lots of research in this area)
- Bucket Spills
  - What if M buckets are not enough?
     Solution: new hash function
  - Families of hash functions  $h_0(\text{key}), h_1(\text{key}), \dots h_n(\text{key})$
  - Transitions only redistribute overflowed buckets





## Extendible Hashing

- Situation: Bucket (primary page) becomes full. Change hashing function and reorganize. Reorganizes index by *doubling* # of buckets
  - Reading and writing all pages is expensive!
- \* <u>Key Idea</u>: Use <u>directory of pointers to buckets</u>, double # of buckets by *doubling the directory*, splitting just the bucket that overflowed!
  - Directory much smaller than file, so doubling it is much cheaper. Only spilt pages are split. *No overflows*!
  - Trick lies in how hash function is adjusted!

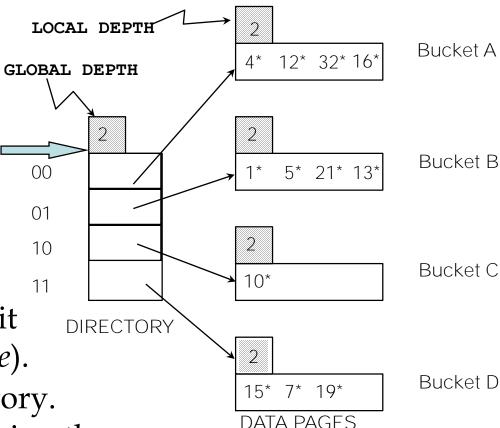




### Example

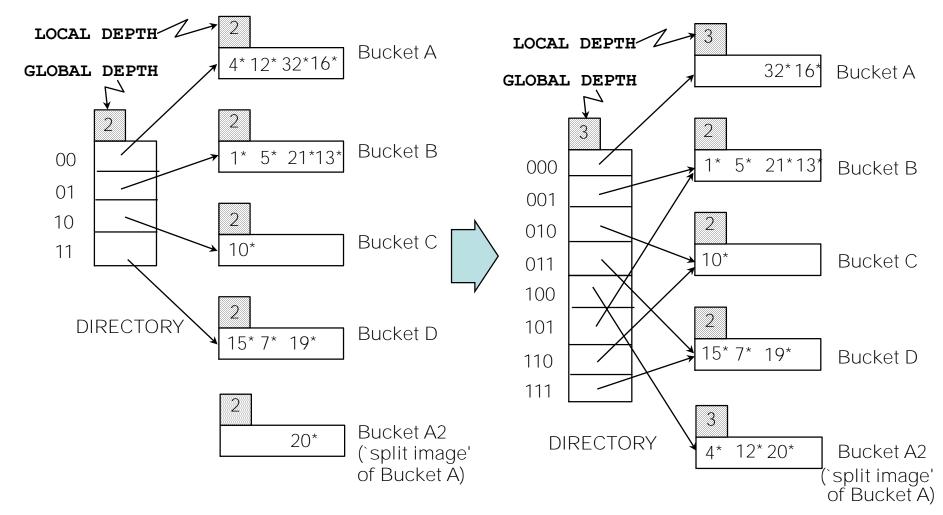
- Directory is array of size 4.
- \* To find bucket for r, take last *global depth* # bits of  $\mathbf{h}(r)$ ; we denote r by  $\mathbf{h}(r)$ .
  - If  $\mathbf{h}(r) = 5 = \text{binary } 101$ , it is in bucket pointed to by 01.
- \* <u>Insert</u>: If bucket is full, <u>split</u> it (allocate new page, re-distribute).
- \* *If necessary*, double the directory.

  (Decision is based on comparing the directory's *global depth* with *local depth* of the bucket.)





# Insert h(r)=20 (Causes Doubling)







### Points to Note

- ❖ 20 = binary 10100. Last 2 bits (00) tell us r belongs in A or A2. Last 3 bits needed to tell which.
  - *Global depth of directory*: Max # of bits needed to tell which bucket an entry belongs to.
  - Local depth of a bucket: # of bits used to determine if an entry belongs to this bucket.
- When does bucket split cause directory doubling?
  - Before insert, local depth of bucket = global depth. Insert causes local depth to become > global depth; directory is doubled by copying it over and 'fixing' pointer to split image page. (Use of least significant bits enables efficient doubling via copying of directory!)



# Comments on Extendible Hashing

- \* If directory fits in memory, equality search answered with one disk access; else two.
  - 100MB file, 100 bytes/rec, 4K pages contains 1,000,000 records (as data entries) and 25,000 directory elements; chances are high that directory will fit in memory.
  - Directory grows in spurts, and, if the distribution *of hash values* is skewed, directory can grow large.
  - Multiple entries with same hash value cause problems!
- ❖ <u>Delete</u>: If removal of data entry makes bucket empty, it can be merged with its 'split image'. If each directory element points to same bucket as its split image, can halve directory.





### Linear Hashing

- This is another dynamic hashing scheme, an alternative to Extendible Hashing.
- \* LH avoids the need for a directory, yet *avoids* the problem of "*long*" overflow chains.
- \* *Idea*: Use a family of hash functions  $\mathbf{h}_0$ ,  $\mathbf{h}_1$ ,  $\mathbf{h}_2$ , ...
  - $\mathbf{h}_{i}(key) = \mathbf{h}(key) \mod(2^{i}N)$ ; N = initial # buckets
  - **h** is some hash function (range is *not* 0 to N-1)
  - If N =  $2^{d0}$ , for some d0,  $\mathbf{h}_i$  consists of applying  $\mathbf{h}$  and looking at the last di bits, where di = d0 + i.
  - $\mathbf{h}_{i+1}$  doubles the range of  $\mathbf{h}_{i}$  (similar to directory doubling)



# Linear Hashing (Contd.)



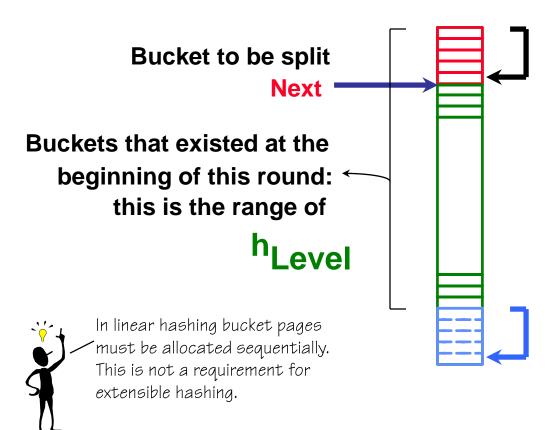
- \* Directory avoided in LH by allowing overflow pages, and always splitting the next bucket (in a round-robin fashion).
  - Splitting proceeds in `rounds'. Round ends when all  $N_R$  initial (for round R) buckets are split. Buckets 0 to  $N_R$  to been split;  $N_R$  yet to be split.
  - Current round number is *Level*.
  - Search: To find bucket for data entry r, find  $\mathbf{h}_{Level}(r)$ :
    - If  $\mathbf{h}_{Level}(r)$  in range Next to  $N_R$ , r belongs here.
    - Else, r could belong to bucket  $\mathbf{h}_{Level}(r)$  or bucket  $\mathbf{h}_{Level}(r) + N_R$ ; must apply  $\mathbf{h}_{Level+1}(r)$  to find out.





### Overview of LH File

In the middle of a round.



Buckets split in this round:

If h<sub>Level</sub> (search key value)
is in this range, must use
h<sub>Level-1</sub>(search key value)
to decide if entry is in
`split image' bucket.

`split image' buckets: created (through splitting of other buckets) in this round





# Linear Hashing (Contd.)

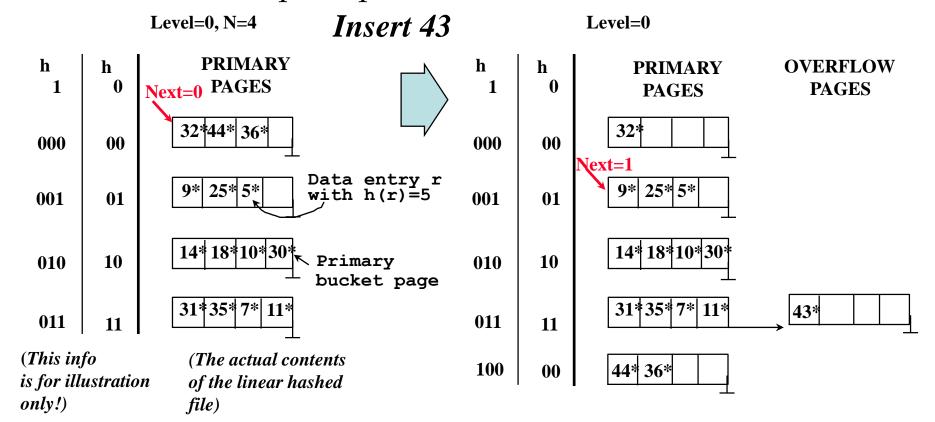
- \* Insert: Find bucket by applying  $\mathbf{h}_{Level}$  /  $\mathbf{h}_{Level+1}$ :
  - If bucket to insert into is full:
    - Add overflow page and insert data entry.
    - Split *Next* bucket and any associated overflow pages and increment *Next*.
    - The bucket that is split may not be the same as the one that overflowed!
- Can choose alternate criterions to 'trigger' split
- Next must be updated sequentially. Since buckets are split round-robin, long overflow chains don't develop!
- Doubling of directory in Extendible Hashing is similar; switching of hash functions is *implicit* in how the # of bits examined is increased





# Example of Linear Hashing

- ❖ On split, h<sub>Level+1</sub> is used to redistribute entries.
- If bucket is full, Spill, Split 'Next', Move 'Next'

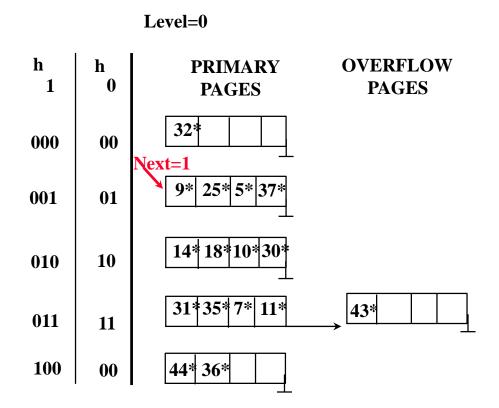






## Insert 37 (00100101)

❖ References page ≥ "Next", check  $h_0$  page, fits, no action







correct bucket.

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### Insert 29 (00011101)

- References page ≥ "Next", check h<sub>0</sub> page
- Spill, split, move Next

Level=0 **OVERFLOW** h **PRIMARY** 0 **PAGES PAGES** h **OVERFLOW** h **PRIMARY** 32\* 0 **PAGES PAGES** 000 00 000 00 25\* 001 01 Next=1 Next=2 25\*|5\*|37\* 001 01 14\* 18\*10\*30\* **10** 010 14\*18\*10\*30\* 10 010 31\*35\*7\* 11\* 43\* 011 11 31\*35\*7\*|11\* 43\* 011 11 100 44\* 36\* If we had inserted '28' instead, then page < Next, so we'd 100 44\* 36\* need to consider h<sub>1</sub> 5\*|37\*|29\* 101 to determine the

Level=0



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### Insert 22 (00010110)

References page ≥ "Next", check h<sub>0</sub> page

spill, split, move Next **OVERFLOW PRIMARY** Level=0 **PAGES PAGES OVERFLOW** h **PRIMARY** 32\* 0 **PAGES PAGES** 000 00 32\* 000 00 9\*| 25\*| 001 01 9\*| 25\*| 001 01 18\* 10\* **10** 010 Next=2 Next=3 14\* 18\*10\*30\* 31\*35\*7\* 11\* 10 010 43\* 011 11 31\*35\*7\*|11\* 43\* 011 100 44\* 36\* 11 100 44\* 36\* 5\*|37\*|29\* 101 5\*|37\*|29\* 101

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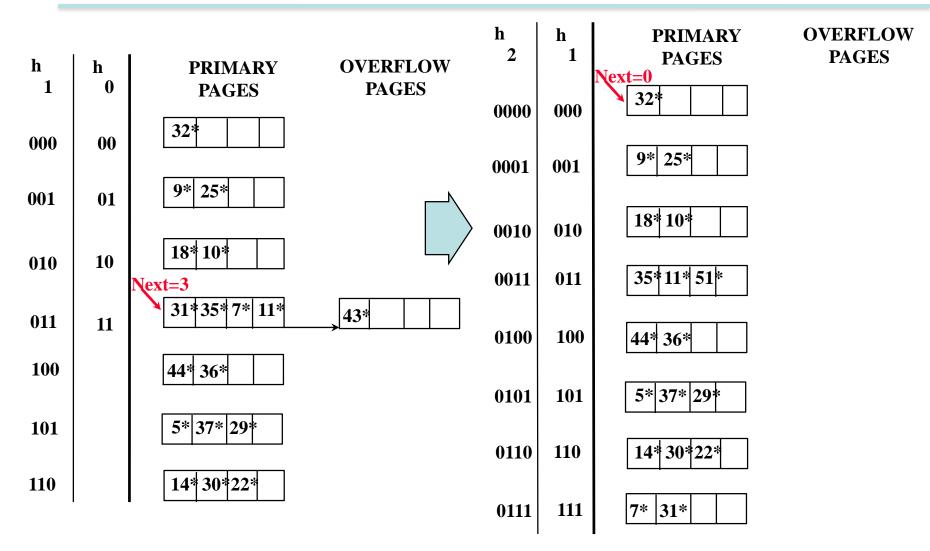
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Level=0

14 \* 30 \* 22 \*



# Add 51 (00110011): End of a Round







### LH Described as a Variant of EH

- The two schemes are actually quite similar:
  - Begin with an EH index where directory has *N* elements.
  - Use overflow pages, split buckets round-robin.
  - First split is at bucket 0. (Imagine directory being doubled at this point.) But elements <1,N+1>, <2,N+2>, ... are the same. So, need only create directory element N, which differs from 0, now.
    - When bucket 1 splits, create directory element N+1, etc.
- \* So, directory can double gradually. Also, primary bucket pages are created in order. If they are *allocated* in sequence too (so that finding i<sup>th</sup> is easy), we actually don't need a directory! Voila, LH.





### Summary

- Hash-based indexes: best for equality searches, cannot support range searches.
- Static Hashing can lead to long overflow chains.
- \* Extendible Hashing avoids overflow pages by splitting a full bucket when a new data entry is to be added to it. (*Duplicates may require overflow pages*.)
  - Directory to keep track of buckets, doubles periodically.
  - Can get large with skewed data; additional I/O if this does not fit in main memory.





### Summary (Contd.)

- Linear Hashing avoids a directory by splitting buckets round-robin, and using overflow pages.
  - Overflow pages not likely to be long, nor around for long.
  - Duplicates handled easily.
  - Space utilization could be lower than Extendible Hashing, since splits not concentrated on `dense' data areas.
    - Can tune criterion for triggering splits to trade-off slightly longer chains for better space utilization.
- \* For hash-based indexes, a *skewed* data distribution is one in which the *hash values* of data entries are not uniformly distributed!